

$j_l$

$$j_0(z) = \frac{\sin z}{z}$$

$$j_1(z) = \frac{\sin z}{z^2} - \frac{\cos z}{z}$$

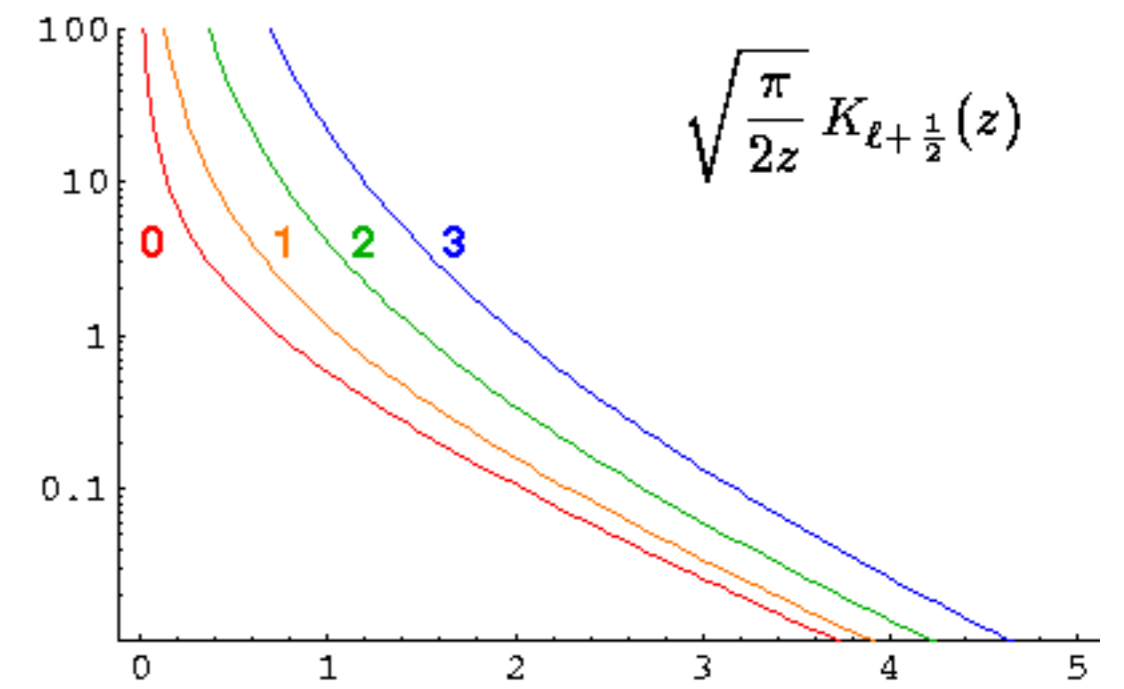
$$j_2(z) = \left(\frac{3}{z^3} - \frac{1}{z}\right) \sin z - \frac{3}{z^2} \cos z$$

$$j_l(z) \begin{cases} \xrightarrow{z \rightarrow 0} \frac{(\frac{1}{2})!}{(l + \frac{1}{2})!} \left(\frac{z}{2}\right)^l = \frac{1}{(\frac{3}{2})_l} \left(\frac{z}{2}\right)^l \\ \xrightarrow{z \rightarrow \infty} \frac{1}{z} \cos\left(z - \frac{\pi}{2}(l+1)\right) \end{cases}$$

$$R(\rho) = N j_l(\rho) = N \frac{(\rho/2)^l (\frac{1}{2})!}{(l + \frac{1}{2})!} {}_0F_1\left(\begin{matrix} - \\ l + \frac{3}{2} \end{matrix}; -\frac{\rho^2}{4}\right)$$

$$j_l(z) = \left(\frac{1}{2}\right)! \sqrt{\frac{2}{z}} J_{l+\frac{1}{2}}(z) = \sqrt{\frac{\pi}{2z}} J_{l+\frac{1}{2}}(z)$$

$$\begin{aligned} &= \pm R(\rho) \\ &= \pm R \\ &= \pm \rho R \\ &\left(-\frac{\partial^2}{\partial \rho^2} - \frac{2}{\rho} \frac{\partial}{\partial \rho} + \frac{l(l+1)}{\rho^2}\right) R(\rho) \\ &= \left(-\frac{\partial^2}{\partial \rho^2} - \frac{2}{\rho} \frac{\partial}{\partial \rho} + \frac{l(l+1)}{\rho^2}\right) R(\rho) \\ &= \left(-\frac{\partial^2}{\partial \rho^2} - \frac{2}{\rho} \frac{\partial}{\partial \rho} + \frac{l(l+1)}{\rho^2}\right) R(\rho) \\ &= \left(-\frac{\partial^2}{\partial \rho^2} - \frac{2}{\rho} \frac{\partial}{\partial \rho} + \frac{l(l+1)}{\rho^2}\right) R(\rho) \end{aligned}$$



$$\sqrt{\frac{\pi}{2z}} K_{l+\frac{1}{2}}(z) \begin{cases} \xrightarrow{z \rightarrow 0} \left(\frac{1}{2}\right)!^2 \frac{(l - \frac{1}{2})!}{(-\frac{1}{2})!} \left(\frac{z}{2}\right)^{l+1} = \frac{\pi}{4} \left(\frac{1}{2}\right)_l \left(\frac{z}{2}\right)^{l+1} \\ \xrightarrow{z \rightarrow \infty} \frac{\pi}{2z} e^{-z} \end{cases}$$

$$\sqrt{\frac{\pi}{2z}} K_{0+\frac{1}{2}}(z) = \frac{\pi}{2z} e^{-z}$$

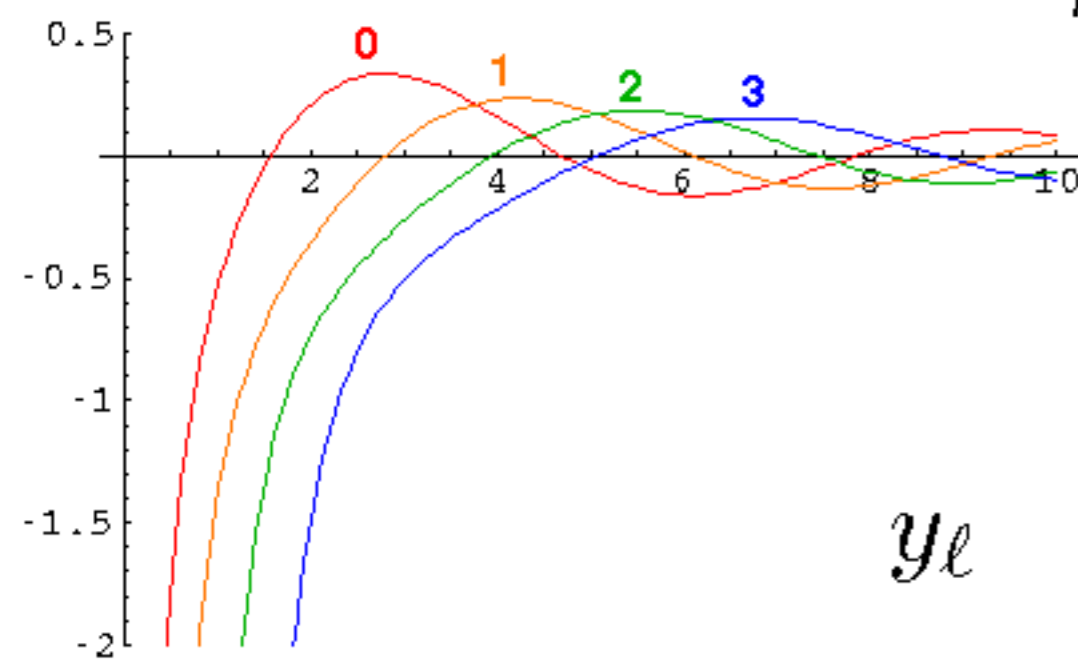
$$\sqrt{\frac{\pi}{2z}} K_{1+\frac{1}{2}}(z) = \frac{\pi}{2z} e^{-z} \left(1 + \frac{1}{z}\right)$$

$$\sqrt{\frac{\pi}{2z}} K_{2+\frac{1}{2}}(z) = \frac{\pi}{2z} e^{-z} \left(1 + \frac{3}{z} + \frac{3}{z^2}\right)$$

$$\sqrt{\frac{\pi}{2z}} I_{l+\frac{1}{2}}(z) \begin{cases} \xrightarrow{z \rightarrow 0} \frac{(\frac{1}{2})!}{(l + \frac{1}{2})!} \left(\frac{z}{2}\right)^l = \frac{1}{(\frac{3}{2})_l} \left(\frac{z}{2}\right)^l \\ \xrightarrow{z \rightarrow \infty} \frac{1}{2z} e^z \end{cases}$$

$$y_l(z) \begin{cases} \xrightarrow{z \rightarrow 0} -\frac{(l - \frac{1}{2})!}{2(-\frac{1}{2})!} \left(\frac{z}{2}\right)^{l+1} = \left(-\frac{1}{2}\right)_{l+1} \left(\frac{z}{2}\right)^{l+1} \\ \xrightarrow{z \rightarrow \infty} \frac{1}{z} \sin\left(z - \frac{\pi}{2}(l+1)\right) \end{cases}$$

$$h_l^{(1,2)}(z) = j_l(z) \pm i y_l(z) \xrightarrow{z \rightarrow \infty} \frac{1}{z} e^{\pm i\left(z - \frac{\pi}{2}(l+1)\right)}$$



$y_l$

$$y_0(z) = -\frac{\cos z}{z}$$

$$y_1(z) = -\frac{\cos z}{z^2} - \frac{\sin z}{z}$$

$$y_2(z) = -\left(\frac{3}{z^3} - \frac{1}{z}\right) \cos z - \frac{3}{z^2} \sin z$$

