

**Physical Constants:**

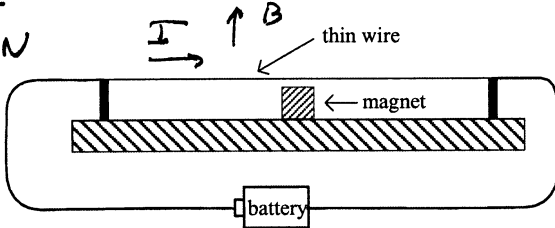
proton charge =  $e = 1.60 \times 10^{-19}$  C

permeability =  $\mu_0 = 4\pi \times 10^{-7}$  T · m/A

Unless otherwise stated, select the letter of the single best answer. Each question is worth 1 point.

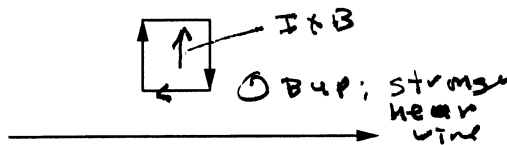
1. The picture below shows a device very similar to one used in class. A battery drives a current through a thin wire which is suspended above a magnet. When the battery is connected the thin wire moves out of the page. What sort of pole is the top of the magnet?

$\vec{B} \uparrow$   
 $\vec{I} \rightarrow$   
 $\vec{F} \text{ out}$   
 $\vec{B} \uparrow \Rightarrow \vec{F} \rightarrow$



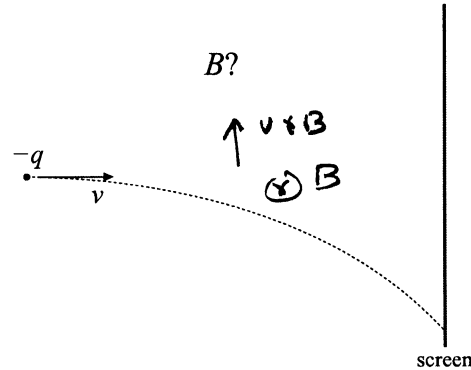
- A. N
- B. S
- C. E
- D. W

2. There is a current flowing clockwise around a square loop and also a current flowing to the right through a long straight wire that sits below the square. (The square loop and the wire sit in the plane of this sheet of paper as shown in the below figure.) The net force on the square points

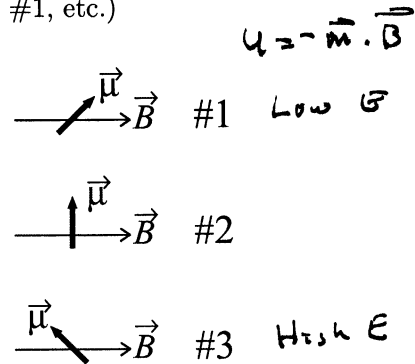


- A. down the page
- B. to the right
- C. out of the page
- D. up the page

3. An electron moves horizontally toward a screen. The electron moves along the dotted path because of a magnetic force caused by a magnetic field. In what direction does that magnetic field point?

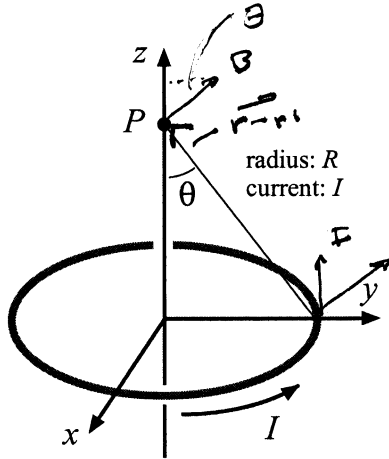


- A. Toward the top of this page
  - B. Toward the bottom of this page
  - C. Into this page
  - D. Out of this page
4. The following figure shows three different configurations of a magnetic dipole  $\vec{\mu}$  placed in a uniform magnetic field  $\vec{B}$ . Which of the below options best describes the relationship between the potential energy of the dipole in these configurations. ( $U_1$  denotes the potential energy in configuration #1, etc.)



- A.  $U_1 > U_2 > U_3$
- B.  $U_1 < U_2 < U_3$
- C.  $U_2 < U_1 < U_3$
- D.  $U_1 = U_3 < U_2$

5. A current  $I$  flows around a circle (radius  $R$ ) that sits in the  $xy$  plane with its center at the origin. Consider the problem of finding the magnitude of the magnetic field,  $B$ , directly above the center, i.e., on the  $z$  axis at a point  $P = (0, 0, z)$ .



~~A~~ Since all of the current elements are the same distance from  $P$ : vector add  $B$

$$B = \frac{\mu_0 I 2\pi R}{4\pi(R^2 + z^2)}$$

~~B~~ Since  $d\vec{\ell} \times \hat{r} = d\ell \sin \theta$   $d\vec{\ell} \perp (\hat{r} - \hat{z})$

$$B = \frac{\mu_0 I 2\pi R \sin \theta}{4\pi(R^2 + z^2)}$$

C Since the net  $B$  field is in the  $z$  direction we need to include the angle:

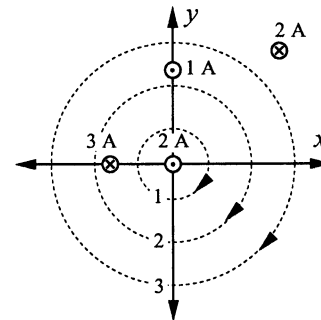
$$B = \frac{\mu_0 I 2\pi R}{4\pi(R^2 + z^2)} \sin \theta$$

~~D~~ Since the net  $B$  field is in the  $z$  direction we need to include the angle:  $\theta = 90^\circ$

$$B = \frac{\mu_0 I 2\pi R}{4\pi(R^2 + z^2)} \cos \theta$$

*show he  
but not  
zero*

6. The below figure shows where four infinitely long wires parallel to the  $z$  axis intersect the  $xy$  plane. The current in each wire is listed along with the flow direction:  $\odot$  = out of page,  $\otimes$  = into page. Consider various amperian loop integrals ( $\mathcal{L} = \oint \vec{B} \cdot d\vec{s}$ ) along three circles centered on the origin with radii as shown in the figure. Which of the below options best describes the relationship between the integrals. ( $\mathcal{L}_1$  denotes the loop integral for circle 1, etc. Negative numbers are smaller than any positive number.)



A.  $\mathcal{L}_1 > \mathcal{L}_3 > \mathcal{L}_2$

B.  $\mathcal{L}_1 > \mathcal{L}_2 > \mathcal{L}_3$

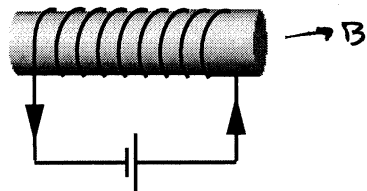
C.  $\mathcal{L}_2 > \mathcal{L}_3 > \mathcal{L}_1$

D.  $\mathcal{L}_3 > \mathcal{L}_2 > \mathcal{L}_1$

sign from rhr

enclosed current:  $\textcircled{1} - 2$   
 $\textcircled{2} + 1$   
 $\textcircled{3} 0$

7.  $N$  turns of wire are wrapped around a cylinder of length  $L$  and radius  $r$  forming a solenoid. The wire carries a current  $I$  in the direction shown. Select the most complete combination of correct statements about this situation.



- I. The magnetic field inside the solenoid points to the left.
- II. Starting at the center of the solenoid and moving to the right along the axis of the solenoid, the magnetic field gradually diminishes, but always points in the same direction.
- III. The magnetic field in the center of the solenoid is proportional to  $I$ .
- IV. If the solenoid is "long" (i.e.,  $L \gg r$ ) the magnetic field in the center of the solenoid is proportional to  $N/L$ .
- V. If the solenoid is "long" (i.e.,  $L \gg r$ ) the magnetic field in the center of the solenoid is inversely proportional to  $r^2 \frac{N}{r} I$

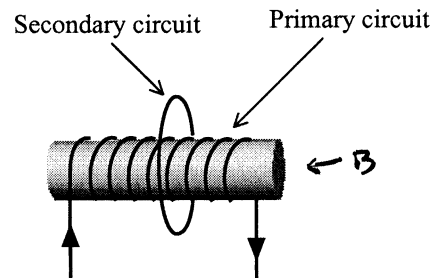
A. I, III

B. II, III, IV

C. III, IV, V

D. I, II, III, IV, V

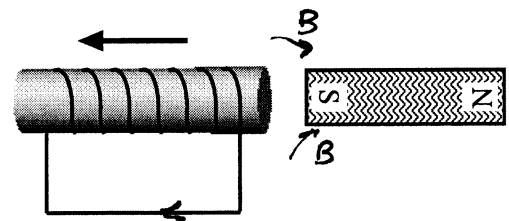
8. (select two answers!) The first circuit consists of a "primary" wrapped around a cylinder and a single-loop "secondary". The current in the primary started at zero but now an ever increasing current is flowing in the direction indicated. What current will be induced in the secondary? At the top of the secondary loop the induced current is flowing:



A. out of the page

B. into the page

In the second circuit a solenoid is moving to the left, away from the south pole of a bar magnet. What induced current will be found in the straight horizontal wire attached to the solenoid? The induced current flows:



C. to the right

D. to the left

#3 By ampere's law, inside  $B = \frac{\mu_0 N I}{2\pi r}$

$dq = S dr$

$$\phi = \int B \cdot dq = \frac{\mu_0 N I}{2\pi} \int_a^{9.15} \frac{1}{r} S dr = \frac{\mu_0 N I S}{2\pi} \ln\left(\frac{9.15}{a}\right)$$

there are  $N$  loops

$$L = \frac{\mu_0 N^2 S}{4\pi \times 10^{-7}} \ln\left(\frac{9.15}{a}\right) = 27.7 \mu H$$