

The $z = 0$ plane is the boundary between two materials: the region of space with $z > 0$ is vacuum, the region with $z < 0$ has $\epsilon = 4\epsilon_0$ and $\mu = 1000\mu_0$. The boundary carries a surface charge density of $\sigma_f = 8.85 \times 10^{-8}$ C/m² and a surface current (flowing in the x direction) of $j_f = 10^3$ A/m. On the vacuum side of the boundary $\vec{E} = 10^3\hat{j} + 10^4\hat{k}$ V/m, and $\vec{B} = -10^{-4}\hat{j} + 10^{-5}\hat{k}$ T. Start by making a sketch showing the directions of the \vec{E} (on both sides) that would result from σ_f in a vacuum. Show on your sketch the direction you are taking for the boundary's normal. Make a sketch showing the direction of \vec{B} (on both sides) that would result from \vec{j}_f in a vacuum. Show on your sketch the direction you are taking for the boundary's tangent. Now find \vec{E} and \vec{B} inside the material. ($\epsilon_0 = 8.85 \times 10^{-12}$ C²/(N · m²) $\mu_0 = 4\pi \times 10^{-7}$ N/A²)

