

Moment of Inertia Tensor of "T"

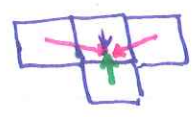


one square: $I_{11} = \sigma \int_{-a/2}^{a/2} \int_{-a/2}^{a/2} y^2 dx dy = \sigma a \frac{y^3}{3} \Big|_{-a/2}^{a/2} = \frac{\sigma a^4}{12} = \frac{M a^2}{12}$

$I_{22} = I_{11}$; $I_{33} = 2 \times I_{11}$; off diagonal = 0

$I = \frac{M a^2}{12} \begin{pmatrix} 1 & & \\ & 1 & \\ & & 2 \end{pmatrix}$

$Y_{cm} = \frac{3 \cdot \frac{a}{2} - \frac{a}{2}}{4} = \frac{a}{4}$



$\vec{a}_1 = (0, -1/4) a$
 $\vec{a}_2 = (0, 3/4) a$
 $\vec{a} = (\pm 1, -1/4) a$

off set vectors:

$I = M a^2 \left\{ \frac{4}{12} \begin{pmatrix} 1 & & \\ & 1 & \\ & & 2 \end{pmatrix} + \sum \left[I \vec{a}_i - \vec{a}_i \vec{a}_i \right] \right\}$
 $\left(\begin{matrix} 1/16 & & \\ & 0 & \\ & & 1/16 \end{matrix} \right) + \left(\begin{matrix} 9/16 & & \\ & 0 & \\ & & 9/16 \end{matrix} \right) + 2 \left(\begin{matrix} 1/16 & & \\ & 1 & \\ & & 17/16 \end{matrix} \right)$

$I_{11} = \frac{1}{3} + \frac{10}{16} + \frac{1}{8} = \frac{17}{12}$

$I_{22} = \frac{1}{3} + 2 = \frac{7}{3}$

$I_{33} = \frac{2}{3} + \frac{10}{16} + \frac{17}{8} = \frac{41}{12}$