

$$I = \frac{12}{6} = 2 \text{ mA} \quad \leftarrow \frac{V}{k\Omega} = \text{mA}$$

energy resistor

$$V_1 = IR_1 = 2 \text{ V}$$

$$V_2 = IR_2 = 4 \text{ V}$$

$$V_3 = IR_3 = 6 \text{ V}$$

$$12 \text{ V}$$

$$P = \frac{V^2}{R} = \frac{12^2}{6 \text{ k}\Omega} = 24 \text{ mW}$$



$$V = 12 \text{ V} \quad \leftarrow \text{energy resistor}$$

$$I_1 = \frac{V}{R_1} = 12 \text{ mA}$$

$$I_2 = \frac{V}{R_2} = 6 \text{ mA}$$

$$I_3 = \frac{V}{R_3} = 4 \text{ mA}$$

$$22 \text{ mA}$$

$$P = V \cdot I = 12 \cdot 22 \text{ mA} = 264 \text{ mW}$$

5)

$$5 \parallel 3 \parallel 2 = \frac{1}{\frac{1}{5} + \frac{1}{3} + \frac{1}{2}} = .9677$$

current thru 7: $\frac{15}{7 + \dots} = 1.883 \text{ mA}$

Volts across 7: $7 \cdot \dots = 13.18 \text{ V} \Rightarrow 15 - 13.18 \text{ across } 5, 3, 2 = 1.822 \text{ V}$

current thru 5: $\frac{1.822}{5} = .364 \text{ mA}$

$$3 = \frac{1.822}{3} = .6073$$

$$2 = \frac{1.822}{2} = .9109$$

$$1.883 \text{ mA}$$

current thru 11 = $\frac{15 \text{ V}}{11} = 1.364 \text{ mA}$

6)

$$P = \frac{V^2}{R} \Rightarrow R = \frac{V^2}{P} = \frac{120^2}{100} = 144 \Omega$$

11) $V = A \sin(\omega t + \phi) + B$

a) DC offset = $B = 1 \text{ V}$

b) amp = $A = 5 \text{ V}$

c) Peak = $A + B = 6 \text{ V}$

d) p-p = $2A = 10 \text{ V}$

c) $rms = \frac{A}{\sqrt{2}} = 3.54 \text{ V}$.435

f) $V = A \sin(\phi) + B = 5 \sin(.45^\circ) + 1 = 3.175 \text{ V}$

g) $F = \frac{\omega}{2\pi} = \frac{1000}{2\pi} = 159 \text{ Hz}$

h) $T = \frac{1}{F} = 6.28 \text{ ms}$

$$13) I = \frac{V}{X_L} = \frac{V}{\omega L} \Rightarrow L = \frac{120V}{20A \cdot 2\pi \cdot 60} = 15.9 \text{ mH}$$

$$= \frac{V}{X_C} = \omega C V \Rightarrow C = \frac{I}{\omega V} = \frac{20A}{2\pi \cdot 60 \cdot 120} = 442 \mu\text{F}$$

Zero power consumed - $V \perp I$ 90° out-of-phase $\langle UI \rangle = 0$

i.e. phase angle $= 90^\circ$ & $\cos(90^\circ) = 0$

$$14) Z_T = R + Z_C + Z_L = 1000\Omega + i \left(\omega L - \frac{1}{\omega C} \right) = 1.59 \text{ k}$$

\uparrow $2\pi \cdot 1000$ \uparrow 10^{-7}
 6.28×10^3

$$= (1, -0.335) \text{ k}$$

$$I = \frac{10}{Z} = (8.99, 3.01) \text{ mA} = 9.48 \angle -32^\circ \text{ mA}$$

phase diff $\neq 0$
 $V \perp I = 18.5^\circ$

$$V_R = RI = (8.99, 3.01) \text{ V} = 9.48 \text{ V}_{\text{rms}}$$

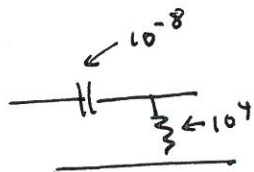
$$V_L = j\omega L \cdot (8.99, 3.01) = (-3.78, 11.3) = 11.9 \angle 109^\circ \text{ V}$$

\uparrow $2\pi \cdot 1000 \cdot 0.02 \Rightarrow 1.257 \text{ k}\Omega$

$$V_C = -\frac{j}{\omega C} (8.99, 3.01) = (4.79, -14.3) = 15.1 \text{ V} \angle -71^\circ \text{ V}$$

note: is add all: $(10, 0) = \text{source!}$

17) High Pass



$$f_{-3dB} = \frac{1}{2\pi RC} = 1.59 \text{ kHz}$$

$$a) I = \frac{V}{R - \frac{j}{\omega C}} = \frac{V/R}{1 - \frac{j}{\omega RC}} = \frac{V/R}{1 - j \frac{f_{-3dB}}{f}} = \frac{1 \text{ mA}}{1 - j \frac{1.59}{1}}$$

$$= \frac{1 \text{ mA}}{1.88 \angle -58^\circ} = 0.532 \text{ mA} \angle +58^\circ$$

phase between V_{in} & V_{out}

$$b) V_R = IR = \frac{V}{1 - j \frac{f_{-3dB}}{f}} = \frac{10V}{1 - j \frac{1.59}{1}} = \frac{10V}{1.88 \angle -58^\circ} = 5.32 \text{ V} \angle +58^\circ \text{ V}$$

$$c) V_C = I \left(-\frac{j}{\omega C} \right) = \frac{V}{1 - j \frac{f_{-3dB}}{f}} \left(-j \frac{f_{-3dB}}{f} \right) = -j \frac{10 \left(\frac{1.59}{1} \right)}{1 - j \frac{1.59}{1}} = \frac{15.9 \angle -90^\circ}{1.88 \angle -58^\circ} = 8.46 \angle -32^\circ \text{ V}$$

Low Pass

$$18) f_{-3dB} = \frac{1}{2\pi RC} = 468 \text{ Hz} = .468 \text{ kHz}$$

\swarrow 50 \nwarrow 6.8×10^{-6}

$$\frac{1}{2\pi RC} = \frac{f_{-3dB}}{f}$$

$$I = \frac{V}{R - \frac{j}{\omega C}} = \frac{V/R}{1 - \frac{j}{\omega RC}} = \frac{V/R}{1 - j \frac{f_{-3dB}}{f}} = \frac{.1/50}{1 - j \frac{.468}{1}}$$

$$= \frac{.1/50}{1.104 \angle -25^\circ} = 1.81 \text{ mA} \angle +25^\circ$$

$$V_R = I \cdot 50 = .0906 \text{ V}$$

$$V_C = \frac{-j}{\omega C} I = \frac{-j}{\omega RC} \frac{V}{1 - \frac{j}{\omega RC}} = -j \frac{f_{-3dB}}{f} \frac{V}{1 - \frac{j}{\omega RC}}$$

$$= \frac{(.1)(.468) \angle -90^\circ}{1.104 \angle -25^\circ} = .0424 \angle -65^\circ \text{ V}$$

\uparrow
 angle between V_{out} & V_{in}

23)



$$P = I^2 R \Rightarrow R = 146 \Omega$$

\uparrow 20W \uparrow .37A

$$\hookrightarrow V_R = (1.46)(.37) = 54 \text{ V}$$

$$I = \frac{V}{R + j\omega L} \Rightarrow |I| = \frac{|V|}{\sqrt{R^2 + \omega^2 L^2}} \text{ or } R^2 + \omega^2 L^2 = \frac{V^2}{I^2}$$

$$\omega^2 L^2 = \frac{V^2}{I^2} - R^2$$

$$L = \frac{1}{\omega} \sqrt{\frac{V^2}{I^2} - R^2}$$

$$= \frac{1}{2\pi \cdot 50} \sqrt{\left(\frac{240}{.37}\right)^2 - 146^2} \rightarrow 632$$

$$= \boxed{2.01 \text{ H}}$$

25) Require $(R + j\omega L) \parallel \frac{-j}{\omega C}$ to be real

$$Z_{net} = \frac{(R + j\omega L) \left(\frac{-j}{\omega C}\right)}{R + j\left(\omega L - \frac{1}{\omega C}\right)} = \frac{+\frac{L}{C} - j\frac{R}{\omega C}}{R + j\left(\omega L - \frac{1}{\omega C}\right)}$$

$$= \frac{R^2 \left(\frac{L}{R^2 C} - j\frac{1}{\omega RC}\right)}{R \left(1 + j\left(\frac{\omega L}{R} - \frac{1}{\omega RC}\right)\right)} = \frac{\frac{L}{C} \left(1 - j\frac{R}{\omega L}\right)}{R \left(1 + j\left(\frac{\omega L}{R} - \frac{1}{\omega RC}\right)\right)}$$

If this is going to be real top & bottom must have same phase $\Rightarrow \frac{R}{\omega L} = \frac{1}{\omega RC} - \frac{\omega L}{R}$

$\omega = 2\pi \cdot 5$
 $L = 2$
 $R = 146 \Omega$

$$\frac{R}{\omega L} + \frac{\omega L}{R} = \frac{1}{\omega RC}$$

$$\omega RC = \frac{1}{\frac{R}{\omega L} + \frac{\omega L}{R}}$$

$$C = \frac{\frac{1}{\omega R}}{\frac{R}{\omega L} + \frac{\omega L}{R}} = \frac{1}{2\pi \cdot 50 \cdot 146} \cdot \frac{2\pi \cdot 50 \cdot 2}{146} = 4.3$$

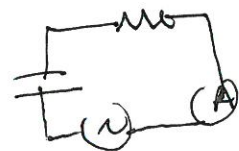
$$= \frac{21.8 \mu F}{4.536} = 4.81 \mu F$$

26) $Z = R + j(\omega L - \frac{1}{\omega C}) = 75 + j \left(10^5 \cdot 10^{-2} - \frac{1}{10^{-8} \cdot 10^5} \right)$
 $= 75 \Omega$

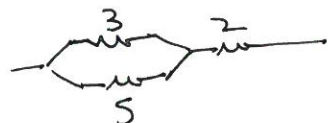
$$V_L = X_L \cdot I = 1k\Omega \cdot \frac{5}{75} = 66.7 V \quad (\text{resonance})$$

(A) shorts out L so circuit is

$$I = \frac{V}{\sqrt{R^2 + \left(\frac{1}{\omega C}\right)^2}} = \frac{V}{\sqrt{75^2 + 1000^2}} \approx 5 mA$$

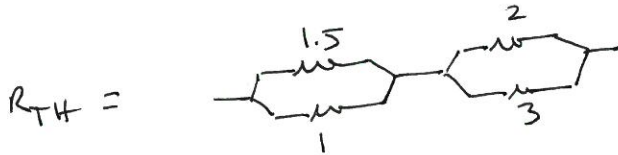


28) (A) $V_{TH} = \frac{5}{8} 12 = 7.5 V$

$R_{TH} =$ 
 $3 || 5 + 2 = \underline{3.875 k\Omega}$

(B) $V_{TH} = \Delta V = \left(\frac{1}{2.5} - \frac{3}{5} \right) 15 V$

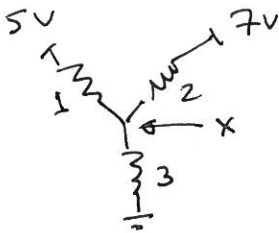
$= \left(\frac{2}{5} - \frac{3}{5} \right) 15 V = -\frac{1}{5} 15 = -3 V$
Just depends on which terminal you call "red"



$1 || 1.5 + 2 || 3 = 1.8 k\Omega$

(C) R_{TH} is easy: $1 || 2 || 3 = \underline{.546 k\Omega}$

V_{TH} is harder - K's Law or I'll use node formula



$\frac{(5-x)}{1} + \frac{(7-x)}{2} + \frac{(0-x)}{3} = 0$

$5 + \frac{7}{2} + 0 = \left(\frac{1}{1} + \frac{1}{2} + \frac{1}{3} \right) x$

$\frac{5 + \frac{7}{2}}{\left(\frac{1}{1} + \frac{1}{2} + \frac{1}{3} \right)} = x = \underline{4.64 V}$

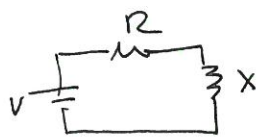
29) $R_{TH} = 2 || 4 = 1.33 k\Omega$

find V_{TH} from current = $\frac{5V}{6\Omega} \rightarrow V_{TH} = 4 \cdot \frac{5}{6} = 3.333$



charges \rightarrow Current = $\frac{\Delta V = 2 \frac{1}{3}}{R = 4 \frac{1}{3}} = \frac{7 \frac{1}{3}}{4 \frac{1}{3}} = \underline{\frac{7}{4} mA}$

1.11:



Power = $I^2 R = \left[\frac{V}{(R+x)} \right]^2 \cdot X = \frac{V^2}{R} \frac{y}{(1+y)^2}$
generic

$f(y) = \frac{y}{(1+y)^2}$

where $y = \frac{x}{R}$

$f'(y) = \frac{1}{(1+y)^2} - \frac{2y}{(1+y)^3} = \frac{1+y-2y}{(1+y)^3} = \frac{1-y}{(1+y)^3}$

$= 0 \rightarrow y =$

